

GOVT.(AUTO) COLLEGE ROURKELA
Sub- Mathematics,Paper-C-4

Answer the followings

No-1

- (a) Write the formula for exponential population growth.
- (b) Give one example of Euler equation.
- (c) What does predatory –prey model describe.
- (d) What is half life in exponential decay.
- (f) What is a phase plane.
- (g) Write two example of exponential decay.
- (h) What do you mean by equilibrium point.
- (i) How drug assimilate into blood.
- (j) What is epidemic model.
- (k) What are the assumptions required for predatory-prey model.
- (l) Check whether the solution of $y'' + 4y = 0$ are independent or not.
- (m) Write word equation for lake pollution model.
- (n) Draw compartmental diagram of lake pollution.
- (o) Write word equation based on balance law drug assimilation into the blood stream.
- (p) Write balance equation in word form for the limited growth with harvesting.
- (q) Formulate the differential equation of simple battle model.
- (s) Find an expression for the time for the population to double in size.
- (t) Define half life .If half cycle is z then find k in terms of z.

Q.No-2

- (a) Find the equilibrium point for the following differential equation $\frac{dX}{dt} = Y - 2XY, \frac{dY}{dt} = XY - Y^2$
- (b) Formulate the differential equation of simple battle model.
- (C) Write the differential equation of Lotka-Volterra Predatory prey system.
- (d) Formulate the differential equation of density-dependent growth model.
- (e) Find an expression for time for the population to double its size.
- (f) What do you mean by epidemic model.
- (g) Solve $(D^2 - 5D + 6)y = e^{2x}$.
- (h) Find the particular integral of $(D^2 + 4)y = \sin x$.
- (i) Write formula for P.I by usin method of variation of parameter.
- (j) Define order and degree of differential equation.

Q.No-3

- (a) Sketch the phase plane trajectory of Battle model.
- (b) How long will it take for the lake pollution level to reach 5% of its initial level if only fresh water flows into the lake.
- (c) Solve $(D^2 + 4)y = \sec x$
- (d) Solve $(D^2 - 6D + 9)y = \sin 2x$
- (e) Solve $(D^2 + 4)y = x \sin x$
- (f) Solve $\frac{d^2y}{dx^2} = \frac{2xy}{x^2 + y^2}$
- (g) Discuss about battle model.

- (h) Find the equilibrium solution of the differential equation of predator-prey model

$$\frac{dX}{dt} = \beta_1 X - C_1 XY$$

$$\frac{dY}{dt} = -\alpha_1 Y + C_2 XY$$

- (i) Use chain rule to find a relation between X and Y from the differential equation

$$\frac{dX}{dt} = -XY, \frac{dY}{dt} = -2Y$$

- (j) Discuss about predator-prey model

No-4

- (i) Solve the differential equation $(2x + \tan y)dx + (x - x^2 \tan y)dy = 0$

- (ii) $(6x + 4y + 1)dx + (4x + 2y + 2)dy = 0$ $y(1) = 2$
- (iii) $dy/dx + 3y/x = 6x^2$
- (iv) Discuss about exponential growth model.
- (v) Solve the initial value problem $D^2y + 4y = \sin x$, $y(0) = 2, y'(0) = 1$
- (vi) Find P.I of $D^2 + 4)Y = x \sin x$
- (vii) Discuss about lake pollution model.
- (viii) Solve $dy/dx - y/x = -y^2/x$
- (ix) $dy/dx + y/2x = x/y^3$, $y(1) = 2$
- (x) Discuss basic properties of linear differential equation.